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EXCLUSIVE GATE COACHING BY IIT/IISC GRADUATES

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# **QUICK REVISION *FORMULA SHEET***

*for*

***GATE -ME REFRIGERATION & AIR-CONDITIONING***





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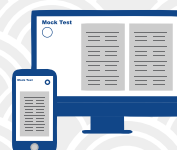
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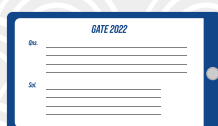
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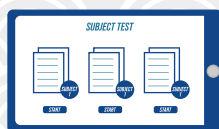
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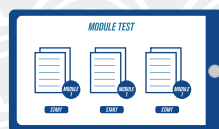
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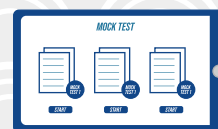
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# REFRIGERATION & AIR-CONDITIONING

## Chapter 1: BASIC CONCEPTS

$$(\text{COP})_{\text{Heat pump}} = \frac{Q_H}{Q_H - Q_L} = \frac{T_H}{T_H - T_L}$$

$$(\text{COP})_{\text{Ref}} = \frac{Q_L}{Q_H - Q_L} = \frac{T_L}{T_H - T_L}$$

$$(\text{COP})_{\text{HP}} = (\text{COP})_{\text{Ref}} + 1 = \frac{1}{\eta_{\text{engine}}}$$

(When working between same temperature limits)

COP = Coefficient of Performance

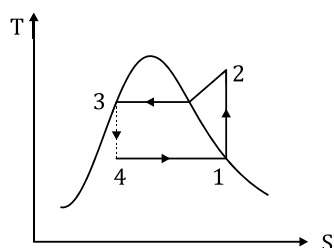
### Unit of Refrigeration:

$$1 \text{ TR} = 3.5167 \text{ kW} = 210 \text{ kJ/min} = 50.4 \text{ kcal/min}$$

1TR: Amount of heat needed to extract from 1000 kg of water at 0°C, to convert it to 1000 kg ice at 0°C in a day (24 hrs).

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## Chapter 2: VAPOUR COMPRESSION REFRIGERATION SYSTEM (VCRS)

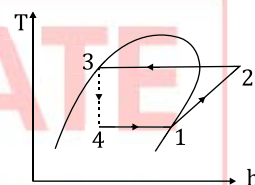
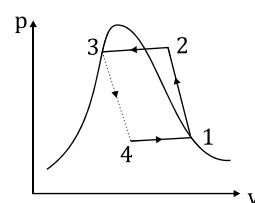
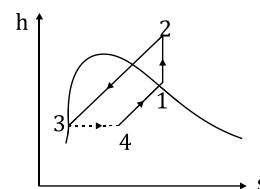


$$(\text{COP}) = \frac{\text{RE}}{W_{\text{input}}} = \frac{h_1 - h_4}{h_2 - h_1}$$

Refrigeration effect = RE

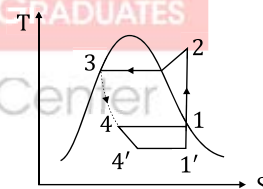
$$= h_1 - h_4 (\text{kJ/kg})$$

$$W_{\text{compressor}} = h_2 - h_1$$



### Modifications in VCRS:

#### 1. ↓ in Evaporator pressure



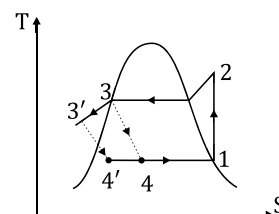
RE ↓

$W_{\text{input}} \uparrow$

$\eta_{\text{vol}} \downarrow$

COP ↓

#### 2. Subcooling:





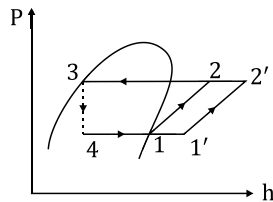
RE ↑

$W_{\text{input}} \rightarrow \text{Same}$

$\eta_{\text{vol}} \rightarrow \text{same}$

COP ↑

### 3. Superheating of Vapour in Evaporator



RE ↑

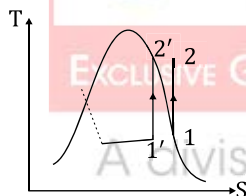
$W_{\text{input}} \uparrow$

COP (may ↓ or ↑)

$\eta_{\text{vol}} \rightarrow \text{Same}$

### Wet vs Dry Compression:

Disadvantages of wet over dry compression

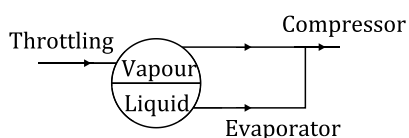


1. RE ↓
2. Refrigerants may wash away the lubricants.
3. Wear and tear
4. Damage compressor valve and body.

### Use of Flash Chamber:

COP → No change

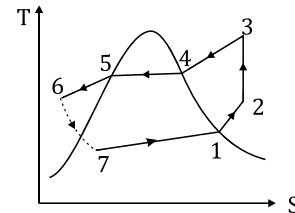
Evaporator size ↓



### Use of Heat Exchanger:

Implies both subcooling and superheating.

Purpose ⇒ to ↓ size of evaporator



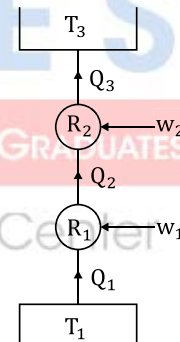
$$h_2 - h_1 = h_5 - h_6$$

$$C_{pv}(T_2 - T_1) = C_{pL}(T_5 - T_6)$$

### Cascade Refrigeration System:

$$(\text{COP})_{\text{CC}} = \frac{(\text{COP})_1 \times (\text{COP})_2}{1 + (\text{COP})_1 + (\text{COP})_2}$$

$$(\text{COP})_{\text{CC}} = \frac{Q_1}{W_1 + W_2}$$



### Volumetric Efficiency:

$$\eta_{\text{vol}} = \frac{\text{Actual volume}}{\text{Theoretical swept volume}}$$

$$\eta_{\text{vol}} = \frac{\dot{m} v_{\text{entry}}}{\frac{\pi}{4} d^2 \ell \times \frac{N}{60} \times K}$$

$$\eta_{\text{vol}} = 1 + C - C \left( \frac{P_H}{P_L} \right)^{\frac{1}{n}}$$

Where  $N = \text{rpm}$

$K = \text{No. of cylinder}$

$v_{\text{entry}}$  = Specific volume at entry of compressor

$$C = \frac{v_c}{v_s}$$

$n$  = Polytropic index

\*\*\*\*\*

## Chapter 3: REFRIGERANTS

### Refrigerants:

Working substance which is used to extract heat from storage space.

#### 1. Primary Refrigerant:

Used directly to absorb heat from storage space by changing their phase ( $L \rightarrow V$ ) in evaporator.

**Eg:** R-11, R-12, R-22, R-134a

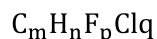
#### 2. Secondary Refrigerant:

Absorbs heat from the storage space and further transfer the same to primary refrigerants.

**Eg:**  $H_2O$ , Brine

### Designation of Refrigerants:

#### a. Saturated Hydrocarbon

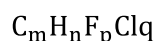


$$\text{Then } n + p + q = 2m + 2$$

$R(m-1)(n+1)p \rightarrow$  Designation.

**Eg:** R-011, R11, R-012, R-134a

#### b. Unsaturated Hydrocarbons:



$$n + p + q = 2m$$

$R 1 (m-1)(n+1)p$

**Eg:** R1150 ( $C_2H_4$ )

#### c. Inorganic Refrigerant:

Designation: R700 + Molecular weight.

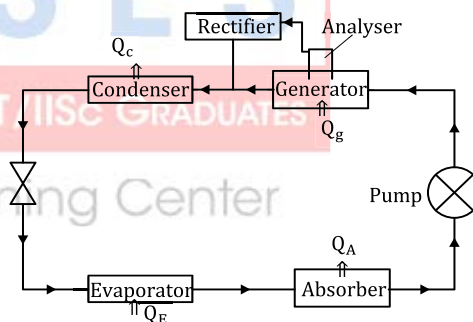
**Eg:**  $NH_3 \rightarrow R717$

### Ozone Depletion:

- Ozone layer is in stratosphere.
- Protects against UV radiation of sun.
- Cl atoms in CFC causes ozone depletion.
- R-134a ( $C_2H_2F_4$ ) is eco-friendly refrigerant.

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## Chapter 4: VAPOUR ABSORPTION REFRIGERATION SYSTEM (VARS)



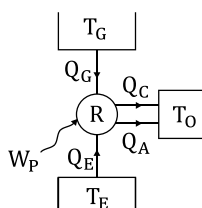
- Compressor is replaced by
  - a. Absorber
  - b. Pump
  - c. Generator
- Heat rejected by refrigerant in absorber and condenser.
- Solar absorption refrigeration system is working on VARS.
- $(COP)_{VARS} = 0.3 \text{ to } 0.5$  (Generally)
- $NH_3 - H_2O$  (ref system)

NH<sub>3</sub> used as refrigerant, H<sub>2</sub>O used as absorber.

- LiBr – H<sub>2</sub>O

H<sub>2</sub>O used as refrigerant.

LiBr used as absorber.



$$((COP)_{VARS})_{\max}$$

$$= \left(1 - \frac{T_O}{T_G}\right) \left(\frac{T_E}{T_O - T_E}\right)$$

⇒ Neglected pumpwork

$$(COP)_{\text{actual}} = \frac{Q_E}{W_P + Q_G}$$

W<sub>P</sub> = Pump work

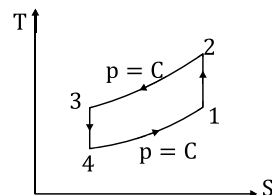
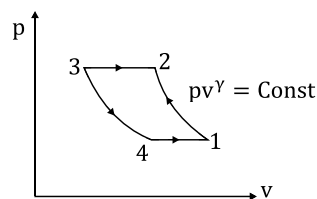
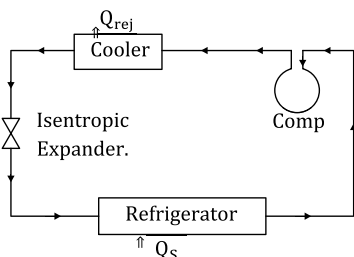
### Electrolux Refrigeration System:

(3 fluid system)

1. NH<sub>3</sub> used as refrigerant.
2. H<sub>2</sub>O used as absorber.
3. H<sub>2</sub> used to reduce partial pressure of NH<sub>3</sub> Vapour.

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## Chapter 5: REVERSE BRAYTON/BELL COLEMAN CYCLE

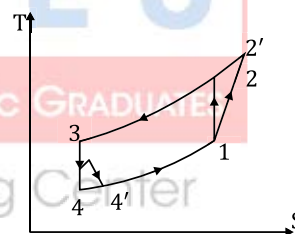


$$r_p = \text{pressure ratio} = \frac{p_H}{p_L}$$

$$(COP)_{RBC} = \frac{1}{\frac{T_2}{T_1} - 1} = \frac{1}{(r_p)^{\frac{\gamma-1}{\gamma}} - 1}$$

This is used when expansion and compression are isentropic.

$$(COP)_{\text{actual}} = \frac{RE}{W_{\text{Comp}} - W_{\text{Expander}}}$$



$$(\eta_{\text{isentropic}})_{\text{Comp}} = \frac{T_2 - T_1}{T'_2 - T_1}$$

$$(\eta_{\text{isentropic}})_{\text{Turbine or Expander}} = \frac{T_3 - T'_4}{T_3 - T_4}$$

$$HRR = \frac{Q_{\text{Condenser}}}{RE}$$

HRR = Heat rejection ratio

RE = Refrigeration effect (process 4-1)

$$(COP)_{\text{Ref}} = \frac{1}{HRR - 1}$$

\*\*\*\*\*



## Chapter 6: AIR CONDITIONING

**Specific Humidity/Humidity Ratio(w)**

$$w = \frac{0.622 p_v}{p_T - p_v}$$

$$\text{Relative humidity } (\phi) = \frac{m_v}{m_{vs}} = P_v/P_{vs}$$

**Wet Bulb Depression (WBD):**

$$\text{WBD} = \text{DBT} - \text{WBT}$$

**Note:**

For saturated air:

$$\text{DBT} = \text{WBT} = \text{DPT}$$

$$\phi = 1 \text{ or } 100\%, \quad p_v = p_{vs}$$

$$\Rightarrow \text{WBD} = 0$$

DBT= dry bulb temperature

DPT = dew point temperature

WBT= wet bulb temperature



**VERY IMPORTANT**

Temp	Temp Notation	Corresponding saturation pressure
DBT	t	$p_{vs}$
WBT	$t'$	$p'_v$
DPT	DPT	$p_v$

**Apjohn Formula (used when WBT is given in the equation):**

$$p_v = p'_v - \frac{1.8p(t - t')}{2700}$$

**Degree of Saturation ( $\mu$ ):**

$$\mu = \frac{w}{w_s}$$

$$\mu = \phi \left( \frac{p - p_{vs}}{p - p_v} \right)$$

**Enthalpy of moist Air (h):**

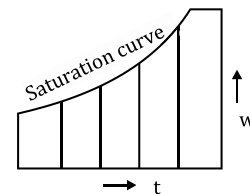
$$h = 1.005t + w(2500 + 1.88t)$$

where  $t = \text{DBT (in } ^\circ\text{C)}$

$w = \text{kg/kg of dry air}$

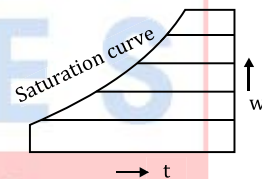
**Various line on Psychrometric Chart:**

a. **Constant DBT Lines:**



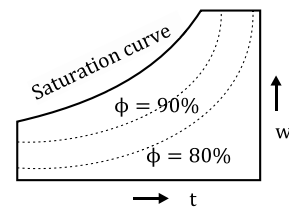
- Uniformly spaced
- Increases in + x direction

b. **Constant Specific Humidity (w) Line:**

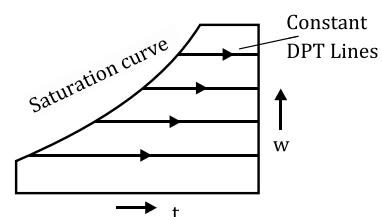


- Uniformly spaced
- increases in + y direction

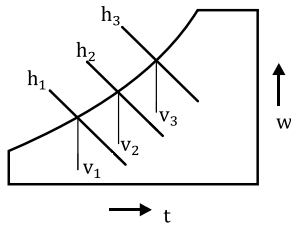
c. **Constant  $\phi$  Line**



d. **Constant DPT Lines**



- Non-uniformly spaced

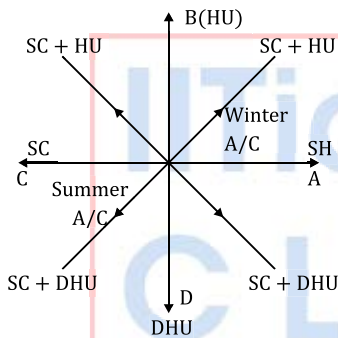


Constant h: Uniformly spaced

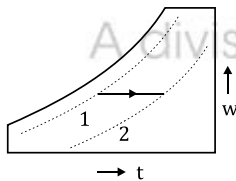
WBT<sub>line</sub>: Non-uniformly spaced

Same degree of inclination.

### Various Psychrometric Processes:

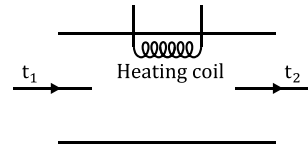


### SH (Sensible Heating):



Effects:

1. Temperature increases
2.  $w = \text{constant}$
3. DPT = constant
4.  $\phi$  decreases
5.  $h$  increases
6. WBT increases,  $v$  increases  
 $v$  (Specific volume)



$$Q_s = m_a(h_1 - h_2)$$

$$Q_s = m_a C_{pa}(t_1 - t_2)$$

$$+ m_v C_{pv}(t_1 - t_2)$$

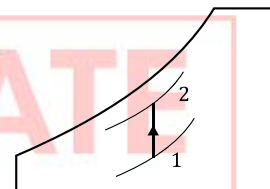
$$Q_s = m_a(1.005 + 1.88w)(t_1 - t_2)$$

Or

$$Q_s = 0.0204 (C_{mm})\Delta t \text{ kW}$$

$$C_{mm} = \text{Volume flow rate of air in m}^3/\text{min}$$

### Humidification (HU):



Effects:

1.  $t = \text{constant}$
2.  $\phi$  increases
3.  $w$  increases  
( $h, \text{WBT}, v$ ) increases
4. DPT increases

$$Q_L = m_a(h_2 - h_1)$$

$$= m_a((C_p t_2 + h_{fg} w_2) - (C_p t_1 + h_{fg} w_1))$$

$$= m_a h_{fg}(w_2 - w_1)$$

$$h_{fg} = \text{Latent heat of vaporization}$$

or

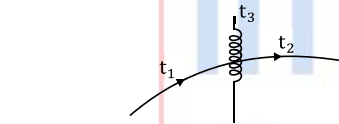
$$Q_L = 50 C_{mm}(\Delta w) \text{ kW}$$

- In desert cooler, cooling and humidification occurs or adiabatic saturation process occurs (i.e., chemical humidification upto saturation curve)
- Chemical humidification and dehumidification are along constant enthalpy lines.

**Sensible Heat Factor(SHF):**

$$SHF = \frac{SH}{SH + LH}$$

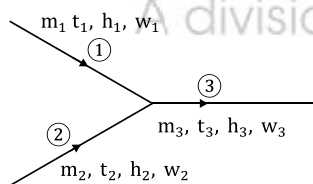
**By Pass Factor (X):**



$$X = \frac{t_3 - t_2}{t_3 - t_1}$$

By pass factor of 'n' coils in series =  $X^n$

**Adiabatic Mixing of Air Streams:**



**Mass Equation:**

- For dry air  
 $m_{a1} + m_{a2} = m_{a3}$  ... eqn 1
- For water Vapour  
 $m_{v1} + m_{v2} = m_{v3}$  ... eqn 2

**Energy Equation:**

$$m_{a1}h_1 + m_{a2}h_2 = (m_{a1} + m_{a2})h_3$$

From equation 2

$$w_1 m_{a1} + w_2 m_{a2} = w_3 (m_{a1} + m_{a2})$$

$$\frac{m_{a1}}{m_{a2}} = \frac{w_3 - w_2}{w_1 - w_3}$$

$$\frac{m_{a1}}{m_{a2}} = \frac{h_3 - h_2}{h_1 - h_3} \approx \frac{t_3 - t_2}{t_1 - t_3}$$

(If only dry air is considered.)

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